Six-degree-of-freedom seismic records in epicentral regions of shallow microearthquakes

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OUTLINE:

- 6DOF Rotaphone
 - basic principles
 - parameters
 - calibration
 - testing

Rotation to translation relations at local distances

- RTR
- equations
- simple models
- Records from microearthquakes
 - West Bohemia (Czech Republic), ML 2.3
 - Gulf of Corinth (Greece), ML 1.9
 - Provadia (Bulgaria), ML 1.6
- Correction of gravity-induced tilt errors in horizontal translational records
- Conclusions

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MISMH

Rotaphone = mechanical sensor system designed to measure spatial ground motion gradients; it consists of sensitive low-frequency geophones, arranged in parallel pairs, connected to a common recording device





horizontal geophones

vertical geophones

Basic features:

The instrument provides collocated records of translational and rotational seismic motions (with the same instrumental characteristics)

The geophones are mounted to a rigid (metal) ground-based frame

Rotation rate is determined by multiple geophone pairs, which allows to perform 'in situ' calibration of the geophones simultaneously with the measurement.





6DOF Seismic Records in epicentral regions of shallow micro-earthquakes



The inversion is performed by the so-called isometric method (Malek et al., 2007), but any other method suitable for weakly nonlinear problems can be used as well.

Specific features and parameters: (component-dependent)

- Dimensions 35 x 35 x 43 cm
 - Weight 9.5 kg
 - Frequency range 2 Hz 60 Hz; upper limit due to the first resonance frequency of the cubic frame (~70 Hz)
 - Dynamic range 120 dB
- ۲
- Largest detectable motion 10⁻¹ m/s (clipping level of the geophones) and 10⁻¹ rad/s
- Least detectable motion 10⁻⁹ m/s, 10⁻⁹ rad/s (theoretical, noise-free); in practice 10⁻⁷ m/s and 10⁻⁷ rad/s (conditioned by the in-situ calibration)

Rotaphone was tested at Albuguerque Seismological Laboratory (ASL), U.S. Geological Survey, New Mexico







(Brokesova et al., 2012b)



Instantaneous, tangential, translational velocity of the Rotaphone (centered 7.62 cm from rotation axis) inferred by direct Rotaphone measurement (black dotted) compared to that obtained from rotation rate and radius (gray) Horizontal-axis shaking, comparing a 16 Hz sinusoidal rotation signal measured by the Rotaphone and FOG

CROSS-AXIS TEST





Array derived rotations (ADR)

(after Spudich et al., JGR, 1995)

$$\mathbf{r}^{i} = (x_{1}^{i}, x_{2}^{i}, 0)^{T} \quad i = 0, 1, \dots, N$$

$$\mathbf{u}^{i} = (u_{1}^{i}, u_{2}^{i}, u_{3}^{i})^{T} \quad \mathbf{d}^{i} = \mathbf{u}^{i} - \mathbf{u}^{0}$$

$$\mathbf{R}^{i} = \mathbf{r}^{i} - \mathbf{r}^{0} \quad \mathbf{d}^{i} = \mathbf{GR}^{i}; \quad G_{ij} = u_{i,j}$$

Spatially uniform displacement gradients !!!

$$\begin{pmatrix} d_1^i \\ d_2^i \\ d_3^i \end{pmatrix} = \begin{pmatrix} u_{1,1} & u_{1,2} & \dots \\ u_{2,1} & u_{2,2} & \dots \\ u_{3,1} & u_{3,2} & \dots \end{pmatrix} \begin{pmatrix} R_1^i \\ R_2^i \\ 0 \end{pmatrix}$$

Minimum number of stations: 3





KLECANY Quarry 25.7.2012, finite differences dv_v/dx and dv_x/dy



KLECANY Quarry 25.7.2012, finite differences dv_z/dx and dv_z/dy



KLECANY Quarry 25.7.2012, Rotaphone vs. ADR vs. R1



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The z-axis rotation rate and the transverse acceleration waveforms coincide. In analogy:

The transverse-axis rotation rate waveform corresponds to the vertical acceleration waveform

$$\Omega_{\eta} = \frac{1}{c} \dot{v}_z$$

 $\Rightarrow \Omega_z =$

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 $\dot{v}_{\eta} = V_{\eta} F'\left(t - \frac{\xi}{c}\right)$

Rotation to translation relations



Rotation to translation relations

Let us assume a point source generating a spherical wave

$$\mathbf{v} = \frac{\mathbf{V}}{r} F\left(t - \frac{r}{\beta}\right)_{r = \sqrt{x^2 + y^2 + z^2}}$$

For example, the **z-axis rotation rate** component reads:

$$\Omega_{z} = \frac{1}{2} \left[\frac{\partial v_{y}}{\partial x} - \frac{\partial v_{x}}{\partial y} \right] = \frac{1}{2} \left[\frac{y}{r^{2}} v_{x} + \frac{y}{\beta r} \dot{v}_{x} - v_{x} V_{x}^{-1} \frac{\partial V_{x}}{\partial y} - \frac{x}{r^{2}} v_{y} - \frac{x}{\beta r} \dot{v}_{y} + v_{y} V_{y}^{-1} \frac{\partial V_{y}}{\partial x} \right]$$
Rotating to the radial and transverse directions ($x \to \xi$ and $y \to \eta$), receiver at $(\xi, 0, z)$.

$$\Omega_{z} = \frac{1}{2} \left[\frac{\partial v_{\eta}}{\partial \xi} - \frac{\partial v_{\xi}}{\partial \eta} \right] = \frac{1}{2} \left[\frac{z}{r^{2}} v_{\eta} V_{\eta}^{-1} \frac{\partial V_{\eta}}{\partial \xi} - \frac{\xi}{r^{2}} v_{\eta} - \frac{\xi}{\beta r} \dot{v}_{\eta} - \frac{1}{\xi} v_{\xi} V_{\xi}^{-1} \frac{\partial V_{\xi}}{\partial \eta} \right]$$

for a large r and a shallow depth $(\xi \approx r)$

$$\Omega_{z} = \frac{1}{2} \left[\frac{\partial v_{\eta}}{\partial \xi} - \frac{\partial v_{\xi}}{\partial \eta} \right] = \frac{1}{2} \left[\frac{z}{r^{2}} v_{\eta} V_{\eta}^{-1} \frac{\partial V_{\eta}}{\partial \xi} - \frac{\xi}{r^{2}} v_{\eta} - \frac{\xi}{\beta r} \dot{v}_{\eta} - \frac{1}{\xi} v_{\xi} V_{\xi}^{-1} \frac{\partial V_{\xi}}{\partial \eta} \right]$$
$$\Omega_{z} \approx -\frac{1}{2\beta} \dot{v}_{\eta}$$

Analogously, the ξ -axis and η -axis rotation rate components can be derived.

Rotation to translation relations



The three constraints hold at any time (as long as the S-wave is separated from other waves in the seimograms).















ANALYTICAL SOLUTION - Uncertainty in depth



RAY SOLUTION – Vertically inhomogeneous model



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$$\Omega_{\eta} = -\frac{\partial v_z}{\partial \xi} = \frac{\xi}{r^2} v_z + \frac{\xi}{\beta r} \dot{v}_z - v_z \bar{V}_z^{-1} \frac{\partial V_z}{\partial \xi}$$

In grey: ray solution for homogeneous halfspace; the same source (center of rotation) at the depth of 5.5 km







How to quantify the importance of rotation versus translation: - we use '**rotation to translation ratio**' (RTR) expressed in rad/m. In our case it relates maximum rotation rate amplitude to maximum translational velocity amplitude **in a given coordinate plane**.



RTR depends on **frequency**, hypocentral distance, source type, radiation pattern, structure along the wavepath, local structure ...

(systematic investigation of many records is necessarry)

Rotaphone at Nový Kostel station (West Bohemia seismic network WEBNET) 2013-01-12 08:54:18 UTC; ML 2.0 Distance from the station **675 m**, depth **9.2 km**, BAZ 205° from North



Intraplate geodynamically active region known for recurrent earthquake swarm activity, CO2 emissions, mineral springs and other post-volcanic events.

Rotaphone at NKC station (West Bohemia seismic network WEBNET) 2013-01-12 08:54:18 UTC; ML 2.0; dist. **0.7 km**, depth **9.2 km**, BAZ 205°



Rotation to translation relations

Rotaphone at NKC station (West Bohemia seismic network WEBNET) 2013-01-12 08:54:18 UTC; ML 2.0; dist. 0.7 km, depth 9.2 km, BAZ 205°

Rotaphone at Sergoula station (Western Greece seismic network PSLNET) 2012-04-25 10:45:22 UTC; ML 2.4

Distance from the station 6.3 km, depth 10.4 km, BAZ 273° from North

Rotaphone at Sergoula station (Western Greece seismic network PSLNET) 2012-04-25 10:45:22 UTC; ML 2.4; dist 6.3 km, depth 10.4 km, BAZ 273°

Rotation to translation relations

CORRELATION NOT GOOD! The applicability of retrieving β is questionable

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Rotaphone at Sergoula station (Western Greece seismic network PSLNET) 2012-04-25 10:45:22 UTC; ML 2.4; dist 6.3 km, depth 10.4 km, BAZ 273°

Rotaphone at Provadia station (Eastern Bulgaria, Provadia local seismic network) 2011-07-11 07:22:47 UTC; ML 1.6

Distance from the station **18.9 km**, depth **2 km**, BAZ 11° from North

Rotaphone at Provadia station (Eastern Bulgaria, Provadia local seismic network) 2011-07-11 07:22:47 UTC; ML 1.6; dist.18.9 km, depth 2 km, BAZ 11°

Rotation to translation relations

$$(\Omega_{\xi}) = \frac{\partial v_z}{\partial \eta} = v_z \bar{V}_z^{-1} \frac{\partial V_z}{\partial \eta},$$

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Rotaphone at Provadia station (Eastern Bulgaria, Provadia local seismic network) 2011-07-11 07:22:47 UTC; ML 1.6; dist.**18.9 km**, depth **2 km**, BAZ 11°

Do tilts contaminate significantly horizontal translational components ?

(the problem discussed, e.g., by Graizer 2005)

 $\Psi_2 \dots$ E-axis tilt

- g ... gravitational acc.
- a_1 ... true horizontal acc.
- a^r , ... recorded 'horizontal' acc.

 $a_1^r = a_1 - g\sin\phi_2 \approx a_1 - g\phi_2$ for small $\phi_2 \quad (\ll 1)$ velocity $v_1^r \approx v_1 - g \int \phi_2 dt; \quad v_1 = \int a_1 dt$

we measure $\Omega_2 = \dot{\phi}_2$, so

(in frequency domain) $... \sim 9.81/(i\omega)^2 \times RTR$

This correction is **NEGLIGIBLE** in our frequency range (above 2 Hz) and for the RTRs recorded up to now (mostly <1)

CONCLUSIONS

- We have developed a 6DOF seismic sensor suitable for field measurements (small size, portability, easy installation and operation)
- Presented prototype is designed to record both weak and strong motions $(10^{-7} 10^{-1} \text{ rad/s})$ in the high frequency range 2 Hz 60 Hz

High accuracy is achieved by the use of our in-situ calibration technique (based on multivaluedness of rotation rate data)

Rotation rate records from local events are extremely variable in overall appearance, namely depending on the source type (anthropogenic/tectonic) and distance.

Three examples of 6DOF records from shallow micro-earthquakes in different seismically active areas were presented (ML 1.6 - 2.4, dist 0.7 -19 km, velocities $10^{-4} - 10^{-6}$ m/s, rot. rates $10^{-5} - 10^{-6}$ rad/s)

We have investigated the rotation to translation relations for small epicentral distances both on synthetic and measured data; application to real seismograms of local shallow earthquakes will be systematically studied in future We define the RTR as the frequency dependent ratio between max.

- amplitude of the corresponding rotation and translation components; above 2 Hz we have mostly found RTR ~ 10^{-1} (rad/m)
- Under such conditions it is not necessary to correct horizontal translational velocity components for the influence of tilts

THANK YOU FOR YOUR ATTENTION

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